

**Focus Topic: 4.1 – Number and Numerical Operations**

TSW = The Student Will

Objective(s)	NJCCCS Alignment	Essential Questions	Understandings	Suggested Assessments
<ul style="list-style-type: none"> <li>• TSW construct meanings for integers, fractions, and decimals</li> </ul>	4.1.6.A.1	<ul style="list-style-type: none"> <li>• How do mathematical ideas interconnect and build on one another to produce a coherent whole?</li> </ul>	<ul style="list-style-type: none"> <li>• One representation may sometimes be more helpful than another.</li> </ul>	Ongoing observation & questioning during class discussions
<ul style="list-style-type: none"> <li>• TSW recognize the decimal nature of currency and compute with money</li> </ul>	4.1.6.A.2	<ul style="list-style-type: none"> <li>• How can we compare and contrast numbers?</li> </ul>	<ul style="list-style-type: none"> <li>• Multiple representations give a fuller understanding of a problem.</li> </ul>	Performance tasks
<ul style="list-style-type: none"> <li>• TSW demonstrate a sense of the relative magnitudes of numbers</li> </ul>	4.1.6.A.3	-	<ul style="list-style-type: none"> <li>•</li> </ul>	Multiple Choice
<ul style="list-style-type: none"> <li>• TSW explore the use ratios and proportions in a variety of situations</li> </ul>	4.1.6.A.4	<ul style="list-style-type: none"> <li>- How can counting, measuring, or labeling help to make sense of the world around us?</li> </ul>	<ul style="list-style-type: none"> <li>• Numeric fluency includes both the understanding of and the ability to appropriately use numbers.</li> </ul>	Literature Connections
<ul style="list-style-type: none"> <li>• TSW use whole number percents between 1 and 100 in a variety of situations</li> </ul>	4.1.6.A.5	<ul style="list-style-type: none"> <li>- How do operations affect numbers?</li> </ul>	<ul style="list-style-type: none"> <li>• There may be multiple algorithms for finding a mathematical solution.</li> </ul>	Short Constructed Responses
<ul style="list-style-type: none"> <li>• TSW use whole numbers, fractions, and decimals to represent equivalent forms of the same number</li> </ul>	4.1.6.A.6	<ul style="list-style-type: none"> <li>- How can we decide when to use an exact answer and when to use an estimate?</li> </ul>	<ul style="list-style-type: none"> <li>• Context is critical when using estimation.</li> </ul>	Extended Constructed Responses
<ul style="list-style-type: none"> <li>• TSW apply number theory concepts in problem solving (primes, factors, multiples, LCM, GCF)</li> </ul>	4.1.6.A.7			Self - Assessment
<ul style="list-style-type: none"> <li>• TSW compare and order numbers</li> </ul>	4.1.6.A.8			
<ul style="list-style-type: none"> <li>• TSW recognize the appropriate use of each arithmetic operation in problem situations</li> </ul>	4.1.6.B.1			
<ul style="list-style-type: none"> <li>• TSW construct and use procedures for calculations with fractions and decimals</li> </ul>	4.1.6.B.2			
<ul style="list-style-type: none"> <li>• TSW use efficient procedures for division of a 3 digit number by a 2 digit number</li> </ul>	4.1.6.B.3			
<ul style="list-style-type: none"> <li>• TSW find squares and cubes of whole numbers</li> </ul>	4.1.6.B.5			

• TSW check the reasonableness of results of computations	4.1.6.B.6			
• TSW understand and use the various relationships among operations and properties of operations	4.1.6.B.7			
• TSW apply standard algebraic orders for the four basic operations, including appropriate use of parentheses	4.1.6.B.8			
• TSW use a variety of estimates for both quantities and computations	4.1.6.C.1			
• TSW recognize when an estimate is appropriate	4.1.6.C.2			
• TSW understand the usefulness of an estimate as distinct from an exact answer	4.1.6.C.2			
• TSW determine the reasonableness of an answer by estimating the result of operations	4.1.6.C.3			
• TSW determine whether a given estimate is an overestimate or an underestimate	4.1.6.C.4			

**Focus Topic: 4.2 – Geometry and Measurement**

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Objective(s)	NJCCCS Alignment	Essential Questions	Understandings	Suggested Assessments
<ul style="list-style-type: none"> <li>TSW understand and apply concepts involving lines:                             <ul style="list-style-type: none"> <li>*Notation for line, ray, angle, line segment</li> <li>*Properties of parallel, perpendicular, and intersecting lines</li> <li>* Sum of the measures of the interior angles of a 180° triangle</li> </ul> </li> </ul>	4.2.6.A.1	<ul style="list-style-type: none"> <li>How can spatial relationships be described by careful use of geometric language?</li> </ul>	<ul style="list-style-type: none"> <li>Geometric properties can be used to construct geometric figures.</li> </ul>	Ongoing observation & questioning during class discussions
<ul style="list-style-type: none"> <li>TSW compare properties of cylinders, prisms, cones, pyramids, and spheres</li> </ul>	4.2.6.A.2	<ul style="list-style-type: none"> <li>How do geometric relationships help us to solve problems?</li> </ul>	<ul style="list-style-type: none"> <li>Shapes and area can be conserved during mathematical transformations.</li> </ul>	Performance tasks
<ul style="list-style-type: none"> <li>TSW identify similar objects</li> </ul>	4.2.6.A.3	<ul style="list-style-type: none"> <li>What situations can be analyzed using transformations and symmetries?</li> </ul>	<ul style="list-style-type: none"> <li>Reasoning can be used to verify or contradict theorems in geometry.</li> </ul>	Short Constructed Responses

<ul style="list-style-type: none"> <li>• TSW understand and apply the concepts of congruence and symmetry (line and rotation)</li> </ul>	4.2.6.A.4	- How can you best represent and verify geometric / algebraic relationships?	<ul style="list-style-type: none"> <li>• Measurement is affected by how an object is measured.</li> </ul>	Extended Constructed Responses
<ul style="list-style-type: none"> <li>• TSW describe and draw the faces or shadows of three-dimensional geometric objects</li> </ul>	4.2.6.A.6	- How can measurement be used to solve problems?		Multiple Choice
<ul style="list-style-type: none"> <li>• TSW identify a three-dimensional shape with given projections</li> </ul>	4.2.6.A.7	- How can measurement be used to solve problem?		Self-Assessment
<ul style="list-style-type: none"> <li>• TSW identify a three-dimensional shape with a given net</li> </ul>	4.2.6.A.8			Literature Connections
<ul style="list-style-type: none"> <li>• TSW use a translation, reflection, or rotation to map one figure onto another congruent figure</li> </ul>	4.2.6.B.1			
<ul style="list-style-type: none"> <li>• TSW recognize, identify, and describe geometric relationships and properties in relation to real world settings</li> </ul>	4.2.6.B.2			
<ul style="list-style-type: none"> <li>• TSW create geometric shapes with specified properties in the first quadrant on a coordinate grid</li> </ul>	4.2.6.C.1			
<ul style="list-style-type: none"> <li>• TSW use appropriate units to measure surface area and volume</li> </ul>	4.2.6.D.1			
<ul style="list-style-type: none"> <li>• TSW use a scale to find a distance on a map</li> </ul>	4.2.5.D.2			
<ul style="list-style-type: none"> <li>• TSW convert measurement systems within a system</li> </ul>	4.2.5.D.3			
<ul style="list-style-type: none"> <li>• TSW know equivalents between standard and metric systems</li> </ul>	4.2.5.D.4			
<ul style="list-style-type: none"> <li>• TSW use measurements and estimates to describe and compare phenomena</li> </ul>	4.2.5.D.5			
<ul style="list-style-type: none"> <li>• TSW use a protractor to measure angles</li> </ul>	4.2.6.E.1			
<ul style="list-style-type: none"> <li>• TSW apply strategies and formulas for finding perimeter and area of: *triangle, square, triangle, parallelogram, trapezoid *circumference and area of a circle</li> </ul>	4.2.6.E.2			

<ul style="list-style-type: none"> <li>• TSW develop and apply strategies and formulas for finding the surface area and volume of rectangular prisms and cylinders</li> </ul>	4.2.6.E.3			
<ul style="list-style-type: none"> <li>• TSW recognize that shapes with the same perimeter do not necessarily have the same area and vice versa</li> </ul>	4.2.6.E.4			
<ul style="list-style-type: none"> <li>• TSW develop ways of approximating the measures of familiar objects</li> </ul>	4.2.6.E.5			

**Focus Topic: 4.3 – Patterns and Algebra**

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Objective(s)	NJCCCS Alignment	Essential Questions	Understandings	Suggested Assessments
<ul style="list-style-type: none"> <li>• TSW provide descriptions of patterns using tables, verbal rules, simple equations, and graphs</li> </ul>	4.3.6.A.1	- How can change be best represented mathematically?	<ul style="list-style-type: none"> <li>• The symbolic language of algebra is used to communicate and generalize the patterns in mathematics.</li> </ul>	Ongoing observation & questioning during class discussions
<ul style="list-style-type: none"> <li>• TSW create patterns involving whole numbers and rational numbers using iterative formulas and recursive patterns</li> </ul>	4.3.6.A.1	- How are patterns of change related to the behavior of functions?	<ul style="list-style-type: none"> <li>• Patterns and relationships can be represented graphically, numerically, symbolically or verbally.</li> </ul>	Performance tasks
<ul style="list-style-type: none"> <li>• TSW describe and create patterns involving whole numbers and rational numbers using recursive patterns, including Pascal’s Triangle</li> </ul>	4.3.6.A.1	- How can we use physical models to clarify mathematical relationships?	<ul style="list-style-type: none"> <li>• Mathematical models can be used to describe and quantify physical relationships.</li> </ul>	Multiple Choice
<ul style="list-style-type: none"> <li>• TSW describe the general behavior of functions given by formulas or verbal rules</li> </ul>	4.3.6.B.1	- What makes an algebraic algorithm both effective and efficient?	<ul style="list-style-type: none"> <li>• Algebraic and numeric procedures are interconnected and build on one another</li> </ul>	Short Constructed Responses
<ul style="list-style-type: none"> <li>• TSW use patterns, relations, and linear functions to model situations using variables to represent unknown quantities</li> </ul>	4.3.6.C.1			Extended Constructed Responses
<ul style="list-style-type: none"> <li>• TSW use patterns, relations, and linear functions to model situations using concrete materials, tables, graphs, verbal rules, algebraic expressions, equations, and inequalities</li> </ul>	4.3.6.C.1			Literature Connections
<ul style="list-style-type: none"> <li>• TSW draw freehand sketches of graphs that model</li> </ul>	4.3.6.C.2			Self-Assessment
<ul style="list-style-type: none"> <li>• TSW graph and interpret relationships between quantities</li> </ul>	4.3.6.C.2			

• TSW graph changes over time	4.3.6.C.2			
• TSW graph rates of change	4.3.6.C.2			
• TSW solve linear equations with whole number coefficients only evaluate numerical expressions	4.3.6.D.1			
• TSW solve linear equations with variables on one or both sides of the equation	4.3.6.D.1			
• TSW apply the properties of operations and numbers using the distributive property	4.3.6.D.2			
• TSW understand the properties of operations and numbers using the product of a number when its reciprocal is 1	4.3.6.D.2			
• TSW evaluate numerical expressions	4.3.6.D.3			
• TSE extend understanding and use inequality	4.3.6.D.4			

**Focus Topic: 4.4 – Data Analysis, Probability, and Discrete Mathematics**

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Objective(s)	NJCCCS Alignment	Essential Questions	Understandings	Suggested Assessments
• TSW collect, generate, organize and display data generated from surveys	4.4.6.A.1	• How can the collection, organization, interpretation, and display of data be used to answer questions?	• Graphs convey data in a precise way.	Ongoing observation & questioning during class discussions
• TSW draw inferences from displays of data using a bar graph, line graph, circle graph, table, and histogram	4.4.6.A.2	• What counting strategy works best here?	• Experimental results tend to approach theoretical probabilities after a large number of trials.	Performance tasks
• TSW read, interpret and construct displays of data using range, median, and mean	4.4.6.A.2	• How can algorithmic thinking be used to solve problems?	• Optimization is finding the best solution within given constraints.	Projects

<ul style="list-style-type: none"> <li>• TSW display data using calculators and computers to record and process information</li> </ul>	4.4.6.A.2	<ul style="list-style-type: none"> <li>• What is the best way to solve this? What counting strategy works best?</li> </ul>		Short Constructed Responses
<ul style="list-style-type: none"> <li>• TSW respond to questions about data</li> </ul>	4.4.6.A.3	<ul style="list-style-type: none"> <li>• How can experimental and theoretical probabilities be used to make predictions or draw conclusions?</li> </ul>		Extended Constructed Responses
<ul style="list-style-type: none"> <li>• TSW generate questions and hypotheses</li> </ul>	4.4.6.A.3			Multiple Choice
<ul style="list-style-type: none"> <li>• TSW formulate strategies for answering questions</li> </ul>	4.4.6.A.3			Self - Assessment
<ul style="list-style-type: none"> <li>• TSW test hypotheses</li> </ul>	4.4.6.A.3			
<ul style="list-style-type: none"> <li>• TSW determine the probability of events using the multiplication rule for probabilities</li> </ul>	4.4.6.B.1			
<ul style="list-style-type: none"> <li>• TSW determine the probability of event and complementary event add up to 1</li> </ul>	4.4.6.B.1			
<ul style="list-style-type: none"> <li>• TSW determine probability using intuitive, experimental, and theoretical methods given numbers of various types</li> </ul>	4.4.6.B.2			
<ul style="list-style-type: none"> <li>• TSW explore compound events</li> </ul>	4.4.6.B.3			
<ul style="list-style-type: none"> <li>• TSW model situations involving probability with simulations</li> </ul>	4.4.6.B.4			
<ul style="list-style-type: none"> <li>• TSW recognize and understand the connections among the concepts of independent outcomes, picking at random, and fairness</li> </ul>	4.4.6.B.5			
<ul style="list-style-type: none"> <li>• TSW use Venn Diagrams to solve counting problems and justify that all possibilities have been calculated without duplication</li> </ul>	4.4.6.C.1			
<ul style="list-style-type: none"> <li>• TSW apply the multiplication principle of counting in simple situations and the number of ways items can be arranged in order</li> </ul>	4.4.6.C.2			
<ul style="list-style-type: none"> <li>• TSW list the possible combinations of two elements chosen from a given set</li> </ul>	4.4.6.C.3			

• TSW devise strategies for winning simple games	4.4.6.D.1			
• TSW analyze vertex edge graphs and tree diagrams	4.4.6.D.2			
• TSW use vertex-edge graphs to represent and find solutions to practical problems	4.4.6.D.3			

**Focus Topic: 4.5 –Mathematical Processes**

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Objective(s)	NJCCCS Alignment	Essential Questions	Understandings	Suggested Assessments
• TSW monitor progress and reflect on the process of problem solving activity	4.5.A.5	• Fully Integrated in above	• Fully Integrated in above	Ongoing observation & questioning during class discussions
• TSW use the language of mathematics to express mathematical ideas precisely	4.5.B.4			Performance tasks
• TSW trace the development of mathematical concepts over time and across cultures	4.5.C.5			Projects
• TSW make and investigate mathematical conjectures	4.5.D.5			Self – Assessment
• TSW use representations to model and interpret physical, social, and mathematical phenomena	4.5.E.3			
• TSW use graphing calculators and computer software to investigate properties of functions and their graphs	4.5.F.5			